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**RESEARCH ARTICLE**

**APPLICATION OF ALGORITHM OF RUNGE-KUTTA METHOD IN MICROBIAL ENTRAINED OIL RECOVERY IN OIL WELLS OF NIGER DELTA IN NIGERIA**

**Ukpaka, C.P.**

Department of Chemical/Petrochemical Engineering, Rivers State University of Science and Technology, Nkpolu, P.M.B. 5080, Port Harcourt, Nigeria.

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**ABSTRACT**

This paper focuses on the mechanisms using algorithm of Runge-Kutta method in monitoring and predicting the microbial entrained oil recovery (MEOR) in Nigeria Delta Oil wells. The microorganisms isolated and identified was cultured as well inoculated into the oil bioreactor set up to examine the degradation of the heavier hydrocarbon, which leads to the production of lighter hydrocarbon considering properties of the enzymes involved in the biodegradation of the heavier hydrocarbon leading to formation of lighter hydrocarbon in the oil, it is suggested that the process build up the pressure of the reservoir in most circumstances. The dynamic models developed in this paper were simulated to study the behaviour of the system. The algorithm of Runge-Kutta method was applied in solving the numerical integral expression obtained from the dynamic models developed. The functional parameters that influence the process were evaluated and a series of test has been carried out in which petroleum hydrocarbon was used as the testing component. All test results revealed that microorganisms are capable of reactivity the oil wells, suggestion that the mechanism of the MEOR process is basically, a simple combination of biodegradation parameters and factors that influence biodegradation process.

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**INTRODUCTION**

The idea of oil recovery using microorganisms has attracted a lot of research interest. The technique varies ranging from injecting dead microbes at various concentrations through sandstones cores aim at achieving the desired plugging. Such investigation as conducted by various research groups yielded little results (Zobell, 1974; Soko, 1987; Jack and Diblasio, 1985; Silfanus, 2001; Bryant and Barchfield, 1989; Aksu, 2005; Acuner and Dilek, 2004; Huo, Kim and Chiang, 1999 and Myslak, 1998). However, one may ask what is the usefulness of the micro organisms? In the Niger Delta, there are several wells that have been abandoned due to low pressure. The low pressure is experienced due to heavier hydrocarbon left over in the reservoir (oil well). The microorganisms isolated identified and characterized are culture and re-introduced into the oil well. Furthermore, when microorganisms are injected into the system (oil well), biochemical processes take place such as: aerobic will oxidize the heavier hydrocarbons to lighter hydrocarbons, both liquid and gases. The gases will generate another pressure and the micro organisms will be left in the oil well for some time so that the bonds of heavier hydrocarbons are broken as well as anaerobic and facultative ascorbic (Rajaguru, Kalaisler, Palanivel, Sulbburam, 2000; Adedayo, Javadpour, Taylor, Aderson, Moo-Young, 2004 and Hsneh and Chen, 2007).

The need to examine the principle of operation of microbial enhanced oil recovery shows that an oil well left over for some period of time can still produce oil. Also, the study has enabled one to know that other lighter hydrocarbons can be produced from the microbial decomposition of heavier hydrocarbons in an oil well. However, various researches have been conducted on the characteristics of oil well in other to decide the suitable micro-organism to perform the function of MEOR in non-producing oil wells in Niger Delta Area of Nigeria. The purpose of this study is to model the microbial activity on oil well for dynamic characterization of influence of microbial entrained oil recovery and applying the suitable mathematical approach in solving the dynamic model for simulation.

The study has several contributions to life and society. The following are contributions to knowledge: which includes, maximizing production of an oil well, to know suitable microorganism for a particular oil well and to reactivate the dead oil well by the action of microorganism. The study was aimed on the dynamics model for characterizing an oil well for the influence of microbial entrained oil recovery and, the solution of the dynamic model. Studies for implementation of various project conducted has been a major concern to resources, particularly addressing issue such as selecting the microbes for the degradation of petroleum hydrocarbon and associated compound (Maier, Kandelbauer, Ertacher, Cavaco-Paulo, Gubitiz, 2004; Wong, Yuen, 1990; Mali Mahajan, Patil,

\*Corresponding author: [chukwuemeka24@yahoo.com](mailto:chukwuemeka24@yahoo.com)

Kulkarni, 2000; Tan, Berger, Slenders, Svileiskaya, Letting, 2000; Wade, 2002; Sonakya, Raizada, Hausner, Wilderer, 2007; Song and Kataya Ma, 2005; Tringe and Rubin, 2005; Vitas, Sabate, Espuny and Solanas, 2005; Wawrik, Kerkhof, Kukur and Zylstra, 2005; Singleton, Furlong; Rathbun; Whitman, 2001; Sambrook, Fristseh and Manialis, 1989). Premuzic and his group used different microbial formulation of thermophilic, acid- and chemophilic, under various experimental conditions of temperature (30 °C — 80 °C). The result of their work revealed that pressure of 12.8 mpa and pH range of 1.5 — 7.5. There are changes in both physical and chemical properties of crude oil. These changes include sulphur and nitrogen associated compounds and various groups. These changes were not limited to lighter hydrocarbons only but also heavy hydrocarbons (Khehra, Sami, Sharma, Vhadhas and Chimno, 2005; Zhang, Chen, Chen, Chang, Hsueh, 2010; Khaild, Arshad and Crowley, 2009; Ghodake, Jadhar, Dawkar, Govindwar 2006, Mazzoli, Pressione, Giuffrida, Fattori and Barelli, 2007).

Although projects on microbial enhance oil recovery may seem to be straight forward, there has been a lot of failures from field test. These failures are attributed to none existence of proper strategy such as reservoir simulation that could predict the microbial metabolic activities. However, another area of interest is the selective plugging of higher permeability zones where slime-producing bacteria were found suitable. This study gave an insight of the plugging technique, despite the failure of the field test (Grifo, Bazzialupo, Di-Serio, Fucelli and Fani, 1995; Banat, Nigam, Singh and Marchant, 1999; Kumar, Tamura, Jakobsen, Nei, 2001; Moutaouakkil, Zeroual, Zohra, Talbi and Lee, 2003; Lee, Malthews, Paviostathis, 2005). However, the efforts in improving microbially enhanced oil recovery like any of the technique needs to be encourage in view of the economic viability and friendliness (O' Donnell, Young, Rushton, Shirley, Crawford, 2007; Pearson, Krantz, Sessions, Dekas, Leavitt, Edwans, 2008; Roling, Milner, Jones, Fratapietro, Swannell, Danel and Head, 2004; Sanche, Ferrer, Vignes, Gareide Oteyza, Gnmalt, Mas, 2006; Tyson, Chapman, Hugenholtz, Allen, Ram, Rechardson, Solovyer, Rubin, Rokhsar, Banfield 2004 and Cheng and Kinkle, 2001; Bryant and Burchfield, 1989; Jack, and Diblasio, 1985; Ukpaka, 2011; Silfanus, 2008).

However, the plugging depends on the average throat size of the pore in the formation, the microbe and the aggregates. The diagram is shown below: Porous The question of plugging of the porous media and the transport phenomena of microbes in the subsurface cannot be separated. This could be explain by the differential movement of the microbes in the columns of the porous media which has severally been demonstrated in sand filters, soil and sandstone (Altas, 1975; Bento, Camargo, Okeke and Frankenberger, 2005; Ferrari, Binnerup, Gillings, 2005; Fierer and Jackson, 2006; Guenero, and Berlanga, 2006; Hack, Zechmeister-Boltenstern, Bodrossy and Sessitsch, 2004; Sokol, 1987; Steven and Raymond, 2007 and Jenneman, Knapp, Melnemej, menzie and Revue, 1984). The sorption and nonsorption of the microbes is associated with forces which could be repulsive or attractive and depends on the type of microbes and adsorbent surface (Hamamura, Olson, Ward and Inskeep, 2006; Handelsman, 2004; Hill, Walsh, Harris, Moffelt, 2003; Huritigand San Schastian, 2005; Kaeberlein, Lewis, Eptem, 2002; Lin, Chung, Kim, Choi, Jang, Chung,

CLo and Lee, 2005 and Margesin, Labbe, Schinner, Greer and Whyte, 2003).

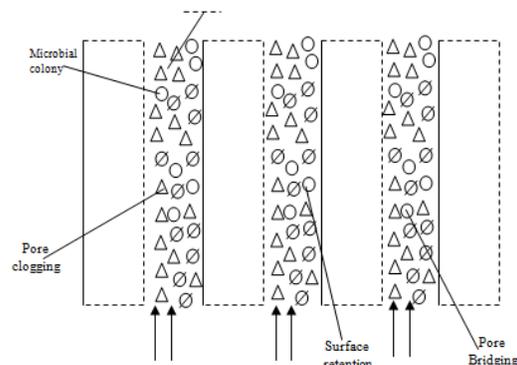


Fig. 1: Plugging in the column of the porous media

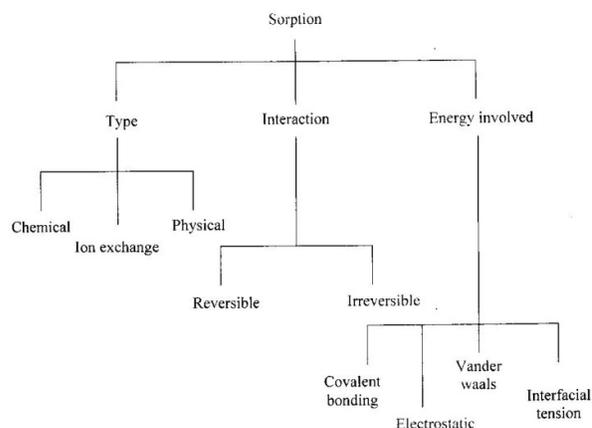


Fig. 2: Forces of sorption

However, a close study of adsorption showed that apart from the surface energies or charges, several forces are responsible for this process. Bitton and Marshall in investigating these force explained that the hydro dynamic and diffusion forces are required to bring the particles to have contact to the sorption surface. A relationship of the force can be illustrated in figure

## MATERIALS AND METHODS

### Materials

The following materials were used in carrying out the research work on the development of mathematical model that will characterize an oil well upon the influence of microbial entrained oil recovery. Reactor Oil well, Microbes, Water and Petroleum product in oil well

### Selecting Microbes

Preliminary studies for implementation of various project conducted shows that a particular microbes has to be selected for the degradation of petroleum hydrocarbon and associated compound. Premuzic and his group had used several microbes (thermophilic, acia-philic and chemophilic) under various experimental conditions of temperature (30°C -80°C). The results of their work revealed that, pressure of 13.8 mpa and

pH range of 1.5-7.5 there are changes in both physical and chemical properties of the crude oil. The microbes used in carrying out the investigation were isolated and identified based on the samples collected from the various oil well. The microbial culture was done using the Buchana and Gibbons, (1974).

### Determination of Microbial and Substrate Concentration

The determination of biomass (microbial) and substrate left after the action of microbes were done using the dynamic models at a particular time. These models were obtained from first principles (material and energy balance) and oil well system. The dynamic models simulated using visual basic 6.0 compiler.

### Mathematical Model Development

When the microbes are added to the oil well to enhance production, the microbes reduces the heavy hydrocarbons into lighter once by biodegradation. However, biodegradation is the removal of organic compounds from oil well by using micro-organism that feeds on the organic compounds. During the process, mineralization, bioaccumulation and polymerization take place. As the micro-organism is inoculated into the oil well containing the necessary nutrients with suitable temperature, pH and pressure, it converts organic substrate into carbon dioxide, and energy is released. At the same time, some of the carbon in the organic substrate was convert to cell constituent, which results to increase in microbial population. As the organic substrate degrades, there is a net loss of live cell mass. Furthermore, the biodegradation process pathway would be: Micro-organism + organic substance - inorganic + new cell (formed) + energy. At intermediate complex is formed during bio-degradation process, is broken down to new cell mass and other products. The biodegradation path could be expressed as:



The accumulation of the biomass on the pore surface is a common experience in microbial enhanced oil recovery. This has been attributed to the biomass growth, retention and detachment. The last two terms are associated with the planktonic phase and sessile phase. Considering the sessile phase Zany presented a biomass conservation equation as follows:

$$T \frac{q(P_B \sigma)}{r_1} = R_r - R_d + R_{BS} \quad (2)$$

### Models of an Oil Well System

Microorganism in activated system like that of sludge experience death at all stages, even at the exponential phase. The crease in the microbial growth rate is proportional tot eh microbial concentration. The first order equation for the general rate of biomass growth is expressed as:

$$\frac{dx}{dt} = R_x = \mu X \quad (3)$$

The specific growth rate  $\mu$  is defined by Monod as;

$$\mu = \mu_{\max} \frac{C_s}{(K_s + C_s)} \quad (4)$$

In biochemical process, a portion of the substrate is used for microbial growth. Hence, in the substrate balance one can make use of the yield, defined as:

$$Y = \frac{\text{mass of cell formed}}{\text{mass of substance consumed}} \quad (5)$$

However, the endogenous decay is the energy required for cell maintenance, death and predation that takes place along side with growth. The net growth rate will be given as:

$$R_x = (\mu - K_d) x \quad (6)$$

where,

$K_d$  = endogenous decay coefficient (per time).

Substituting equation (6) into (4).

$$R_x = \left[ \mu_{\max} \frac{C_s}{(K_s + C_s)} - K_d \right] x \quad (7)$$

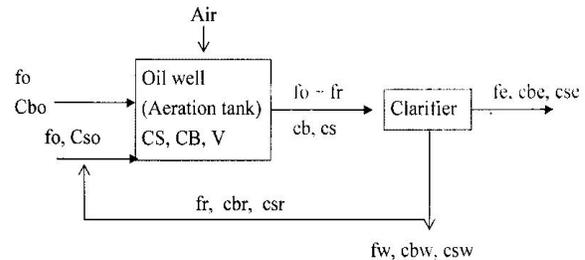


Fig. 3: Hypothetical representation of an oil well system

where,  $f_o$ ,  $c_{so}$ ,  $C_{8o}$  are the inlet flow rate, initial concentration substrate and biomass.

$V$  = volume of the reactor

$C, CB$  = Concentration of substrate and biomass

$F_e, C_{se}, C_{be}$  = effluent flow rate, concentration of substrate and biomass in the effluent stream.

$F_w, C_{sw}, C_{bw}$  = flow rate of the waste stream, concentration of the substrate and biomass in the waste stream.  $F_r, C_{sr}, C_{br}$  = flow rate of the recycled sludge, concentration of the substrate and biomass in the recycled sludge. Also, no microbial activities occur in the clarifier.

### Mass Balance

The principle of conservation of mass is used to determine the component mass balance for the substrate and biomass and it is given as

$$\begin{aligned} \text{Rate of accumulation in} &= \text{Rate of input of} & - & \text{Rate of output of} & + & \text{Rate of} \\ \text{the oil well} & \text{substance in the} & \text{substance in the} & \text{generation/co} \\ \text{system} & \text{oil well system} & \text{oil well system} & \text{consumption of} \\ & & & \text{oil well system} & & \end{aligned} \quad (8)$$

### Mass Balance for Microbes (Biomass)

$$\frac{V_d C_b}{dt} = f_o C_{Bo} + F_R C_r - (f_o + f_r) C_B + R_{CB} V \quad (9)$$

It is assumed that the biomass in the inlet stream is sterile, so CBO = 0

$$\frac{V_d C_b}{dt} = f_o C_{Bo} - F_R C_r - (f_o + f_r) C_B + R_{CB} V \quad (10)$$

Let  $\frac{V}{f_o} = \theta$ ,  $\frac{F_R}{f_o} = \alpha$  and dividing equation (7) by  $f_o$

$$\alpha C_{Br} - (1 + \alpha) C_B + R_{CB} \theta \quad (11)$$

Where,  $\theta$  and  $\alpha$  are the hydraulic retention time and recycle ratio respectively.

Therefore, equation (12) can be written in terms of changes in the hydraulic retention time, which gives the expression in equation (13).

$$\frac{dC_b}{dt} = \frac{\alpha C_{Br}}{\theta} - \frac{(1 + \alpha) C_B}{\theta} + R_{CB} \quad (13)$$

Where  $R_{CB} = R_x$ , which is the rate of reaction of the biomass (microbes).

Substitute equation (7) into (13), the equation becomes.

$$\frac{dC_b}{dt} = \frac{\alpha C_{Br}}{\theta} - \frac{(1 + \alpha) C_B}{\theta} + \left[ \mu_{max} \frac{C_b}{K_s + C_b} - K_d \right] x \quad (14)$$

#### Mass Balance for Substrate (A Hydrocarbons)

$$\frac{V dC_s}{dt} = f_o C_{so} + (f_r + C_{sr}) - (f_o + f_r) C_s + R_{CS} V \quad (15)$$

The biodegradation takes place in the oil well. That means the concentration of the substrate leaving the oil well is the same as that in the clarifier system and effluent i.e  $C_s = C_{SR} = C_{CE}$

$$\frac{V dc_s}{dt} = f_o C_{so} - f_o C_s + R_{cs} V \quad (16)$$

Divide equation 12 by V

$$\frac{dC_s}{dt} = \frac{f_o C_{so} - f_o C_s}{V} - R_{cs} \quad (17)$$

$$\frac{dC_s}{dt} = \frac{f_o}{V} (C_{so} - C_s) - R_{cs} \quad (18)$$

Where,  $R_{cs}$  is defined as the maximum rate of the substrate (oil or hydrocarbons) utilization per mass of the biomass (microbes).

$$R_{cs} = \frac{\mu x}{y} \quad (19)$$

Combining equations (19) and (4) we have

$$R_{cs} = \frac{x}{y} \left( \mu_{max} \frac{C_s}{K_s + C_s} \right) \quad (20)$$

Substitute equation (20) into (18), the equation becomes:

$$\frac{dC_s}{dt} = \frac{f_o}{V} (C_{so} - C_s) - \left( \frac{\mu_{max} C_s X}{Y(K_s + C_s)} \right) \quad (21)$$

Equations (14) and (21) are dynamic models for the concentration of the biomass (microbes) and substrate (hydrocarbon) for the oil well.

#### Solution Technique

The numerical integral of the developed models can be taken when  $C_{Bo}$ ,  $C_{Br}$ ,  $C_{So}$ ,  $K_d$ ,  $f_o$ ,  $f_r$ ,  $V$ ,  $K_s$  and  $\mu_{max}$  as well as the steady state values for the ordinary differential equations are given and fourth order Runge Kutta method is used to solve the dynamic models.

#### Algorithm of Runge-Kutta Method

The algorithm computes the solution of the initial value problems as:

$$\gamma^1 f(x, y) \text{ and } y(x_0) = y_0 \text{ at } h, \quad (22)$$

$$\text{So that } x_1 = x_0 + h, x_2 = x_0 + 2h, \quad (23)$$

$$x_3 = x_0 + 3h \dots X_n = X_0 + nh \quad (24)$$

where, f is such function or equation developed with solution on the interval  $(X_0, X_n)$  for input: Initial values  $x_0, y_0$  at step size, h for number of steps n. For output: approximate  $y_{n+1} = x_n + nh$

where

$$n = 0, 1, 2 \dots n-1 \quad (25)$$

$$K_1 = hf(x_i, y_i) \quad (26)$$

$$K_2 = hf(x_i + h/2, y_i + K_1/2) \quad (27)$$

$$K_3 = hf(x_i + h/2, y_i + K_2/2) \quad (28)$$

$$K_4 = hf(x_i + h, y_i + K_3) \quad (29)$$

$$y_{i+1} = y_i + 6/h (K_1 + 2K_2 + 2K_3 + K_4) \quad (30)$$

$$x_{i+1} = x_i + h \quad (31)$$

where i is the number of iteration(s) and the models are solved using this algorithm for the visual Basic 6.0 program.

#### Obtained Parameters

The tables below shows the data or parameter needed to compute the dynamic models in the computer program.

Table 1: Inputs for Biomass (microbes)

Input variables	Input values
Concentration of biomass, CB (Mg/l)	2400
Concentration recycle biomass, CBr	1429.17
Hydraulic retention time, $\theta$	21.8
Recycle ratio, $\alpha$	0.81818181
Saturation constant $K_s$	3.0
Endogenous decay, $K_d$	0.1
Monond constant $\mu_{max}$	0.3398
Biomass concentration X	2400

#### RESULTS AND DISCUSSION

A Compaq Desktop (Intel, Pentium 4) and visual basic 6.0 compiler were used to develop a computer program for the simulation of dynamic models developed. The results showed that the biodegradation of the hydrocarbons (oil) predicted by

the model was close to that of plant data obtained. The model prediction shows a deviation of 3.10% from the plant data obtained. Table 4 below shows the model result with plant data, as well as percentage deviation.

**Table 2: Input for substrate (hydrocarbons)**

Input variables	Input values
Flow rate of substrate $f_0$	0.055
Volume of oil well, V (L)	1.2
Initial concentration of substrate, CSo (Mg/L)	250
Concentration of substrate, Cs (mg/L)	250
Saturation constant $K_s$	3.0
Monod constant $\mu_{max}$	0.3398
Yield coefficient $y$ (mg cell/ mg substrate)	1.2
Biomass concentration X	

**Table 3: Plant data with microbial growth**

Inputs	Influent concentration (mg/L)	Plantdata (mg/L)
Hydrocarbon	250	0.050
Biomass	2400	

**Table 4: Comparison of Model Results with Plant Data**

Inputs	Influent concentration (mg/L)	Model prediction of the effluent (Mg/L)	Deviation (%)	Plant data (mg/L)
Hydrocarbons	250	0.0516	3.10	0.050
Biomass	2400			

The result shows that the substrate (oil) concentration decreases from initial value of 250 mg/L at time,  $t = 0$  to 0.0516 mg/L at time,  $t = 0.49$  hours. At this stage, the concentration of the hydrocarbon substrate is low meaning that the microbes or microorganism have converted the bond of heavy hydrocarbons in oil well to lighter hydrocarbons. These lighter hydrocarbons which are gases will generate pressure so that the oil well can produce again. The products of oil well are water, gases and oil (hydrocarbons).

**Effects of Microbes on Substrate Concentration**

The simulation of the models shows that as time increase, the substrate or hydrocarbon concentration decreases, Figure 4 shows the variation of substrate (hydrocarbon) concentration with time.

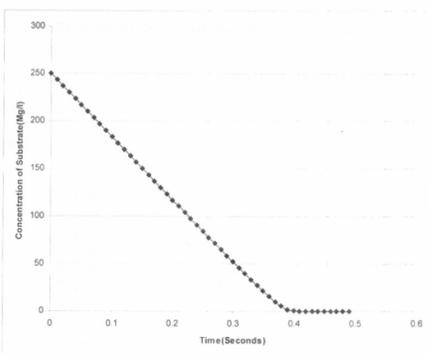


Fig. 4.1 Variation of Substrate (hydrocarbon) Concentration with time

However, the decrease in concentration of substrate or hydrocarbon is as a result of the action of the microbes, what makes the oil well not to produce normally is too much heavy

hydrocarbon left in the oil well. The microbes were injected into the oil well and allowed for some time to degrade or breakdown the heavy bonds of the hydrocarbons to a lighter one. At time,  $t = 0.45$  hour(s), the concentration was slightly constant.

**Effectiveness of Biomass (Microbes)**

The result of the model shows that as time increases, the biomass concentration increases as well. Figure 5 shows the variation of Biomass (microbes) concentration with time.

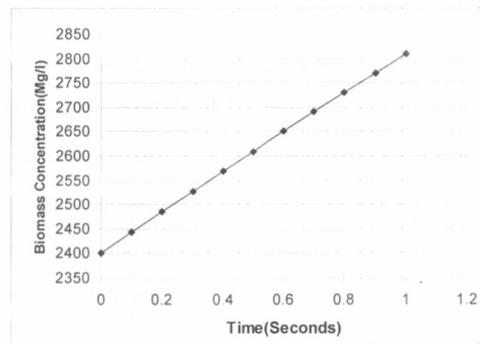


Fig. 5: Variation of Biomass (Microbes) Concentration with time

However, the increase in concentration of biomass (microbe) with increase in time is due to conversion of the hydrocarbon (substrate) into carbon dioxide and energy is release. At the same time, the microbes concern some of the carbon in the organic substrate to cell constituent which results to increase in microbial population.

**Model Simulation**

The dynamic models developed were simulated to study the behaviour of the system. The effect varying saturation constant ( $K_s$ ) to see how concentration will change with time for substrate (hydrocarbon) and biomass (microbes) was conducted (microbes).

**Effect of Saturation Constant on Biomass Concentration with Time**

It was observed that as saturated constant ( $K_s$ ) was increased to  $K_s = 4.0$ , the biomass concentration increased further with time. Figure 3 shows the effect of saturation constant on the biomass concentration with time.

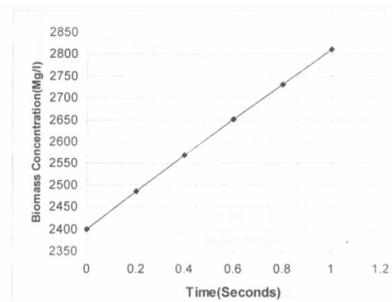


Figure 6: Effect of Saturation Constant Concentration with time on the Biomass

From the above graph, the increase in biomass concentration with time increases the microbial population, which means for the microbial population to increase so as to enhance biodegradation of the hydrocarbons (substrate), the saturation constant should be increased.

### Effect of Saturation Constant on Substrate Concentration with Time

It was also observed that as saturation constant ( $K_s$ ) was changed to  $K_s = 4.0$ , the substrate (hydrocarbon) concentration decreases. Figure 7 shows the effect of saturation constant on the substrate concentration with time.

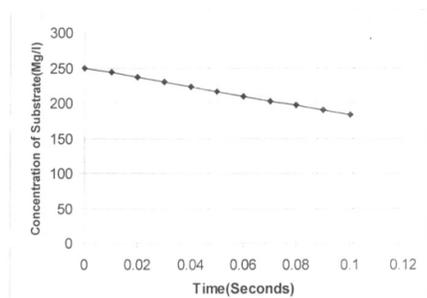


Figure 7: Effect of saturation constant on the Substrate Concentration with time

From the figure 7 above, the decrease in substrate concentration was as a result of increase in microbial population with increase in saturation constant ( $K_s$ ) to four more microbes now feed on the substrate with time.

### Conclusion

Most oil wells are left over for years without production, not that these oil wells do not have needed hydrocarbons. However, these oil wells can be made to produce again with the influence of microbial entrained oil recovery, by this one means the use of microorganisms to enhance the biodegradation of some hydrocarbons in the oil well especially the heavy ones and also production of such oil well. Furthermore, two dynamic models were developed from first principle by applying material balance principle. Michael Menten enzyme kinetic model and biodegradation kinetics were also used in developing the models. Also, the models were solved by writing a program with visual basic 6 - 0 compilers using the fourth order Runge Kutta algorithm. The result obtained from the model simulation was close to plant data obtained. The biomass (microbes) degrades the hydrocarbon from 250 mg/L at time,  $t = 0$  to 0.0516 mg/L at time,  $t = 0.49$  hours. The result shows that after 0.49 hours, the oil well was able to produce and the deviation was 3.10% from plant data.

### Nomenclature

$\alpha$	=	pore fraction occupied by the retained biomass (dimensionless)
$P_B$	=	mass density of the biomass (mg/l)
$R_r$	=	biomass retention (cell mg/day)
$R_d$	=	Biomass detachment (cell mg/day)
$R_{BS}$	=	Biomass growth (cell mg/l <sub>3</sub> /day)

$\Delta$	=	nutrient (mg)
$\alpha$	=	recycle ratio (dimensionless)
$\phi$	=	oil (mg)
$\theta$	=	hydraulic retention time (day <sup>-1</sup> )
O	=	microbe (cell mg)
$F_0, F_R, F_T$	=	volumetric flow rate (m <sup>3</sup> /day)
x	=	cell mass/unit culture volume (cell mg/l)
$K_s$	=	Saturated constant (mg/l)
$C_s$	=	substrate concentration (mg/day)
$R_s$	=	specific rate of the substrate (mg/day)
S	=	substrate concentration (mg%)
$\mu_{max}$	=	maximum specific rate of microbial growth (cell mg/day)
$\mu$	=	specific rate of microbial growth (cell mg/day)
$R_x$	=	specific rate of the biomass (cell mg/day)
$K_d$	=	equilibrium constant of decay rate
Y	=	yield coefficient

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